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**Exercise – 9.1**

1. In a  $\triangle ABC$ , if  $\angle A = 55^\circ$ ,  $\angle B = 40^\circ$ , find  $\angle C$ .

**Sol:**

Given  $\angle A = 55^\circ$ ,  $\angle B = 40^\circ$  then  $\angle C = ?$

We know that

In  $\triangle ABC$  sum of all angles of triangle is  $180^\circ$

$$\text{i.e., } \angle A + \angle B + \angle C = 180^\circ$$

$$\Rightarrow 55^\circ + 40^\circ + \angle C = 180^\circ$$

$$\Rightarrow 95^\circ + \angle C = 180^\circ$$

$$\Rightarrow \angle C = 180^\circ - 95^\circ$$

$$\Rightarrow \angle C = 85^\circ$$

2. If the angles of a triangle are in the ratio 1 : 2 : 3, determine three angles.

**Sol:**

Given that the angles of a triangle are in the ratio 1 : 2 : 3

Let the angles be  $a, 2a, 3a$

$\therefore$  We know that

Sum of all angles of triangles is  $180^\circ$

$$a + 2a + 3a = 180^\circ$$

$$\Rightarrow 6a = 180^\circ$$

$$\Rightarrow a = \frac{180^\circ}{6}$$

$$\Rightarrow a = 30^\circ$$

Since  $a = 30^\circ$

$$2a = 2(30)^\circ = 60^\circ$$

$$3a = 3(30)^\circ = 90^\circ$$

$\therefore$  angles are  $a = 30^\circ, 2a = 60^\circ, 3a = 90^\circ$

$\therefore$  Hence angles are  $30^\circ, 60^\circ$  and  $90^\circ$

3. The angles of a triangle are  $(x - 40)^\circ$ ,  $(x - 20)^\circ$  and  $(\frac{1}{2}x - 10)^\circ$ . Find the value of  $x$ .

**Sol:**

Given that

The angles of a triangle are

$$(x - 40)^\circ, (x - 20)^\circ \text{ and } \left(\frac{x}{2} - 10\right)^\circ$$

We know that

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Sum of all angles of triangle is  $180^\circ$

$$\therefore x - 40^\circ + x - 20^\circ + \frac{x}{2} - 10^\circ = 180^\circ$$

$$2x + \frac{x}{2} - 70^\circ = 180^\circ$$

$$\frac{5x}{2} = 180 + 70^\circ$$

$$5x = 250^\circ (2)$$

$$x = 50^\circ (2)$$

$$x = 100^\circ$$

$$\therefore x = 100^\circ$$

4. The angles of a triangle are arranged in ascending order of magnitude. If the difference between two consecutive angles is  $10^\circ$ , find the three angles.

**Sol:**

Given that,

The difference between two consecutive angles is  $10^\circ$

Let  $x, x+10, x+20$  be the consecutive angles differ by  $10^\circ$

*W · K · T* sum of all angles of triangle is  $180^\circ$

$$x + x + 10 + x + 20 = 180^\circ$$

$$3x + 30 = 180^\circ$$

$$\Rightarrow 3x = 180 - 30^\circ \Rightarrow 3x = 150^\circ$$

$$\Rightarrow x = 50^\circ$$

$$\therefore x = 50^\circ$$

$\therefore$  The required angles are

$x, x+10$  and  $x+20$

$$x = 50$$

$$x + 10 = 50 + 10 = 60$$

$$x + 20 = 50 + 10 + 10 = 70$$

The difference between two consecutive angles is  $10^\circ$  then three angles are  $50^\circ, 60^\circ$  and  $70^\circ$ .

5. Two angles of a triangle are equal and the third angle is greater than each of those angles by  $30^\circ$ . Determine all the angles of the triangle.

**Sol:**

Given that,

Two angles are equal and the third angle is greater than each of those angles by  $30^\circ$ .

Let  $x, x, x+30$  be the angles of a triangle

We know that

Sum of all angles of a triangle is  $180^\circ$

$$x + x + x + 30 = 180^\circ$$

$$3x + 30 = 180^\circ$$

$$\Rightarrow 3x = 180^\circ - 30^\circ$$

$$\Rightarrow 3x = 150^\circ$$

$$\Rightarrow x = \frac{150^\circ}{3}$$

$$\Rightarrow x = 50^\circ$$

$\therefore$  The angles are  $x, x, x + 30$

$$x = 50^\circ$$

$$x + 30 = 80^\circ$$

$\therefore$  The required angles are  $50^\circ, 50^\circ, 80^\circ$

6. If one angle of a triangle is equal to the sum of the other two, show that the triangle is a right triangle.

**Sol:**

If one angle of a triangle is equal to the sum of other two

$$\text{i.e., } \angle B = \angle A + \angle C$$

Now, in  $\triangle ABC$

(Sum of all angles of triangle  $180^\circ$ )

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle B + \angle B = 180^\circ \quad [\because \angle B = \angle A + \angle C]$$

$$2\angle B = 180^\circ$$

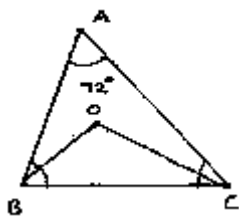
$$\angle B = \frac{180^\circ}{2}$$

$$\angle B = 90^\circ$$

$\therefore ABC$  is a right angled a triangle.

7.  $ABC$  is a triangle in which  $\angle A = 72^\circ$ , the internal bisectors of angles  $B$  and  $C$  meet in  $O$ . Find the magnitude of  $\angle ROC$ .

**Sol:**



Given,

$ABC$  is a triangle

$\angle A = 72^\circ$  and internal bisector of angles  $B$  and  $C$  meeting  $O$

$$\text{In } \triangle ABC = \angle A + \angle B + \angle C = 180^\circ$$

$$\Rightarrow 72^\circ + \angle B + \angle C = 180^\circ$$

$$\Rightarrow \angle B + \angle C = 180^\circ - 72^\circ \text{ divide both sides by '2'}$$

$$\Rightarrow \frac{\angle B}{2} + \frac{\angle C}{2} = \frac{108^\circ}{2} \quad \dots\dots(1)$$

$$\Rightarrow \angle OBC + \angle OCB = 54^\circ \quad \dots\dots(1)$$

$$\text{Now in } \triangle BOC \Rightarrow \angle OBC + \angle OCB + \angle BOC = 180^\circ$$

$$\Rightarrow 54^\circ + \angle BOC = 180^\circ$$

$$\Rightarrow \angle BOC = 180^\circ - 54^\circ = 126^\circ$$

$$\therefore \angle BOC = 126^\circ$$

8. The bisectors of base angles of a triangle cannot enclose a right angle in any case.

**Sol:**

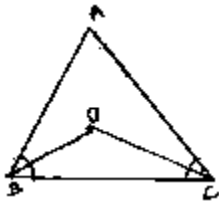
In a  $\triangle ABC$

Sum of all angles of triangles is  $180^\circ$

i.e.,  $\angle A + \angle B + \angle C = 180^\circ$  divide both sides by '2'

$$\Rightarrow \frac{1}{2} \angle A + \frac{1}{2} \angle B + \frac{1}{2} \angle C = 90^\circ$$

$$\Rightarrow \frac{1}{2} \angle A + \angle OBC + \angle OCB = 90^\circ \quad [ \because OB, OC \text{ bisect } \angle B \text{ and } \angle C ]$$



$$\Rightarrow \angle OBC + \angle OCB = 90^\circ - \frac{1}{2} \angle A$$

Now in  $\triangle BOC$

$$\therefore \angle BOC + \angle OBC + \angle OCB = 180^\circ$$

$$\Rightarrow \angle BOC + 90^\circ - \frac{1}{2} \angle A = 180^\circ$$

$$\Rightarrow \angle BOC = 90^\circ - \frac{1}{2} \angle A$$

Hence, bisectors of a base angle cannot enclose right angle.

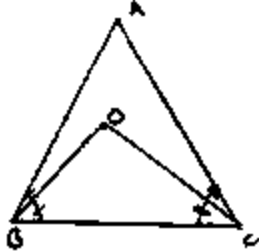
9. If the bisectors of the base angles of a triangle enclose an angle of  $135^\circ$ , prove that the triangle is a right triangle.

**Sol:**

Given the bisectors the base angles of an triangle enclose an angle of  $135^\circ$

i.e.,  $\angle BOC = 135^\circ$

But, W.K.T



$$\angle BOC = 90^\circ + \frac{1}{2} \angle A$$

$$\Rightarrow 135^\circ = 90^\circ + \frac{1}{2} \angle A$$

$$\Rightarrow \frac{1}{2} \angle A = 135^\circ - 90^\circ$$

$$\Rightarrow \angle A = 45^\circ (2)$$

$$\Rightarrow \angle A = 90^\circ$$

$\therefore \triangle ABC$  is right angled triangle right angled at A.

10. In a  $\triangle ABC$ ,  $\angle ABC = \angle ACB$  and the bisectors of  $\angle ABC$  and  $\angle ACB$  intersect at O such that  $\angle BOC = 120^\circ$ . Show that  $\angle A = \angle B = \angle C = 60^\circ$ .

**Sol:**

Given,

In  $\triangle ABC$

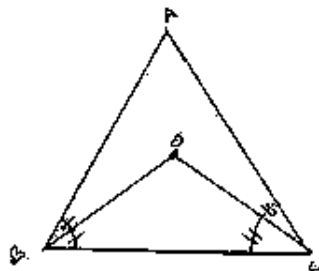
$$\angle ABC = \angle ACB$$

Divide both sides by '2'

$$\frac{1}{2} \angle ABC = \frac{1}{2} \angle ACB$$

$$\Rightarrow \angle OBC = \angle OCB$$

[  $\because OB, OC$  bisects  $\angle B$  and  $\angle C$  ]



Now

$$\angle BOC = 90^\circ + \frac{1}{2} \angle A$$

$$\Rightarrow 120^\circ - 90^\circ = \frac{1}{2} \angle A$$

$$\Rightarrow 30^\circ \times (2) = \angle A$$

$$\Rightarrow \angle A = 60^\circ$$

Now in  $\triangle ABC$

$$\angle A + \angle ABC + \angle ACB = 180^\circ \quad (\text{Sum of all angles of a triangle})$$

$$\Rightarrow 60^\circ + 2\angle ABC = 180^\circ \quad [\because \angle ABC = \angle ACB]$$

$$\Rightarrow 2\angle ABC = 180^\circ - 60^\circ$$

$$\Rightarrow \angle ABC = \frac{120^\circ}{2} = 60^\circ$$

$$\Rightarrow \angle ABC = \angle ACB$$

$$\therefore \angle ACB = 60^\circ$$

Hence proved.

11. Can a triangle have:

- |                         |  |
|-------------------------|--|
| (i) Two right angles?   | (iv) All angles more than $60^\circ$ ? |
| (ii) Two obtuse angles? | (v) All angles less than $60^\circ$ ?  |
| (iii) Two acute angles? | (vi) All angles equal to $60^\circ$ ?  |

Justify your answer in each case.

**Sol:**

(i) No,

Two right angles would up to  $180^\circ$ , So the third angle becomes zero. This is not possible, so a triangle cannot have two right angles.

[Since sum of angles in a triangle is  $180^\circ$ ]

(ii) No,

A triangle can't have 2 obtuse angles. Obtuse angle means more than  $90^\circ$  So that the sum of the two sides will exceed  $180^\circ$  which is not possible. As the sum of all three angles of a triangle is  $180^\circ$ .

(iii) Yes

A triangle can have 2 acute angle. Acute angle means less the  $90^\circ$  angle

(iv) No,

Having angles-more than  $60^\circ$  make that sum more than  $18^\circ$ . Which is not possible

[ $\because$  The sum of all the internal angles of a triangle is  $180^\circ$ ]

- (v) No,  
Having all angles less than  $60^\circ$  will make that sum less than  $180^\circ$  which is not possible.  
[ $\because$  The sum of all the internal angles of a triangle is  $180^\circ$  ]
- (vi) Yes  
A triangle can have three angles are equal to  $60^\circ$  . Then the sum of three angles equal to the  $180^\circ$ . Which is possible such triangles are called as equilateral triangle.  
[ $\because$  The sum of all the internal angles of a triangle is  $180^\circ$  ]

12. If each angle of a triangle is less than the sum of the other two, show that the triangle is acute angled.

**Sol:**

Given each angle of a triangle less than the sum of the other two

$$\therefore \angle A + \angle B + \angle C$$

$$\Rightarrow \angle A + \angle A < \angle A + \angle B + \angle C$$

$$\Rightarrow 2\angle A < 180^\circ \quad \text{[Sum of all angles of a triangle]}$$

$$\Rightarrow \angle A < 90^\circ$$

Similarly  $\angle B < 90^\circ$  and  $\angle C < 90^\circ$

Hence, the triangles acute angled.

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